

The Many Tentacles of Estimands: Patient-Reported Outcomes, Real-World Evidence, Health Economics and Outcomes Research, and Beyond

Lightning Introduction to the Potential Outcomes Framework

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Polling Question



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- ☐ Have you heard of the potential outcomes framework?

Goal



- We are interested in learning about the effect of intervention (W) on an outcome (Y)
- Possible clinical outcomes
 - ▣ Mortality
 - ▣ Progression free survival
- Possible patient reported outcomes (PROs)
 - ▣ Time to clinically meaningful improvement in fatigue
 - ▣ Patient Quality of Life 3 months after initiation
- Possible system performance outcomes
 - ▣ Healthcare expenditures

Intervention



- Causality is tied to an action (or manipulation, treatment, or intervention)
- Example:
 - ▣ Ibrutinib combined with bendamustine and rituximab – **add-on therapy**
 - ▣ **Placebo**, bendamustine, and rituximab



Potential Outcomes

- **Key question: what *would* have happened, under a different treatment?**
- A potential outcome is the value of the outcome variable for a given value of the treatment
- $Y(\text{add-on}) = \text{Fatigue improvement at 3 months (Y/N)}$
- $Y(\text{Placebo}) = \text{Fatigue improvement at 3 months (Y/N)}$
- Possibilities:
 - $Y(\text{add-on}) = \text{N}, Y(\text{Placebo}) = \text{Y}$ **Placebo better**
 - $Y(\text{add-on}) = \text{Y}, Y(\text{Placebo}) = \text{N}$ **Add-on better**
 - $Y(\text{add-on}) = Y(\text{Placebo}) = \text{Y}$
 - $Y(\text{add-on}) = Y(\text{Placebo}) = \text{N}$



No causal effect

Causal Effects



- The **causal effect** is the comparison of the potential outcome under the different treatments
- The mathematical description by which we compare those potential outcomes are called **estimands**.
- A possible estimand with quantitative potential outcomes is $Y(\text{add-on}) - Y(\text{placebo})$

- These are unit-level causal effect
- Unit: the person, place, or thing upon which the treatment will operate, *at a particular point in time*
- Note: the same person at different points in time = different units
- With quantitative outcomes, the causal effect will probably not be the same for each unit (treatment effect heterogeneity)

Estimation



- For the **definition** of a causal effect we compare potential outcomes for a single unit
- However, in reality, we can only see **one** potential outcome for each unit
- For **estimation** of a causal effect we need to consider multiple units,
 - ▣ Need to compare **similar** units, some exposed to either of the possible treatments
 - ▣ Can be same units at different points in time, or different units at the same point in time

Potential Outcomes with Two Units



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- $Y_1(\text{add-on}, \text{add-on}) = \text{Fatigue } Y/N$
- $Y_1(\text{add-on}, \text{Placebo}) = \text{Fatigue } Y/N$
- $Y_1(\text{Placebo}, \text{add-on}) = \text{Fatigue } Y/N$
- $Y_1(\text{Placebo}, \text{Placebo}) = \text{Fatigue } Y/N$
- $Y_2(\text{add-on}, \text{add-on}) = \text{Fatigue } Y/N$
- $Y_2(\text{add-on}, \text{Placebo}) = \text{Fatigue } Y/N$
- $Y_2(\text{Placebo}, \text{add-on}) = \text{Fatigue } Y/N$
- $Y_2(\text{Placebo}, \text{Placebo}) = \text{Fatigue } Y/N$
- **Worse problem**

- Often we need to make assumptions, without which we cannot perform further analyses
- A common assumption is the **Stable Unit Treatment Value Assumption (SUTVA)**

SUTVA (cont.)



- SUTVA has two components:
 - ▣ *No interference* (units do not interfere with each other): treatment applied to one unit does not effect the outcome for another unit
 - ▣ There is only a single version of each treatment level (potential outcomes must be well defined)
- It cannot be verified from the data, and are based entirely on subject matter knowledge and reasoning
 - ▣ Many randomized trials are designed such that SUTVA is plausible

Covariates



- When dealing with multiple units one way to distinguish between units are with covariates.
- A set of variables that are unaffected by the treatment.
- May be related to treatment assignment and/or the outcome
- Usually they are defined by X .

The Observed Data



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Patient #	Covariates (X)	Treatment Received (T)	Potential Outcomes		Outcomes Treatment 2
			Outcomes Treatment 0	Outcomes Treatment 1	
1	X_1	0	$Y_1(0)$	?	?
...	...	...	...	?	?
n_1	X_{n_1}	0	$Y_{n_1}(0)$	?	?
n_1+1	X_{n_1+1}	1	?	$Y_{n_1+1}(1)$	?
...	...	...	...	...	?
n_1+n_2	$X_{n_1+n_2}$	1	?	$Y_{n_1+n_2}(1)$	?
n_1+n_2+1	$X_{n_1+n_2+1}$	2	?	?	$Y_{n_1+n_2+1}(2)$
...	...	...	?	...	...
N	X_N	2	?	?	$Y_N(2)$

The Estimands



- Unit level effects
 - $Y_i(s)$ vs. $Y_i(t)$, $\forall s, t \in \{1, \dots, D\}$
- Population level effects
 - The average difference $\frac{1}{N} \sum_{i=1}^N (Y_i(1) - Y_i(0))$
 - The median difference $\text{median}(Y_i(1) - Y_i(0))$
 - The odds ratio when the outcome is binary
 - The average effect among women
 - The average effect within temperature classes
 - Odds ratio for men

Estimands - PRO



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- PROs may introduce additional complexities that commonly arise from intercurrent events
 - ▣ For example, patients are unable to respond
- Possible estimands:
 - ▣ While on treatment
 - When the outcome are events $E(Y_i(s)/t_i - Y_i(t)/t_i)$
 - ▣ Principal Stratification
 - Estimate the effect only among those that survive under both treatments
 - ▣ Hypothetical
 - Estimate the effect assuming plausible patients outcomes after intercurrent event.

Estimands – PRO (cont.)



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□ Possible estimands:

▣ Composite estimands

- Assume that either intercurrent event or lack of improvement in fatigue are bad outcome

▣ Intention to Treat

- In some cases it is possible to observe the PRO even after intercurrent event (e.g. change of drug). A possible estimand is $E(Y_i(s) - Y_i(t))$.