

PCN440

Network Meta-Analysis Using Fractional Polynomials:
Heuristic for Model Selection Incorporating
Beyond-Trial Extrapolations (A Melanoma Example)

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Background

- Fractional polynomials (FP) provide flexible parametric modeling approaches for analyzing time-to-event data
- In FP models, the log hazard of an event, such as all-cause mortality, is fit as a function of time using parametric models of the form
$$\log \text{ hazard} = (\mu_0) + (\mu_1) t^{P1} + (\mu_2) t^{P2},$$
where μ_0 represents the scale parameter, μ_1 and μ_2 represent shape parameters, t represents time, and $P1$ and $P2$ are powers from the set (eg, $\{-1, -0.5, 0, 0.5, 1\}$), and where $t^0 = \ln(t)$. When $P1 = P2 = P$, the model becomes a repeated powers model
$$\log \text{ hazard} = (\mu_0) + (\mu_1) t^P + (\mu_2) t^P \ln(t)$$
- To capture treatment effects, differences (d) can be added to the first, second, and/or third term of FP models
$$\log \text{ hazard} = (\mu_0 + d_0) + (\mu_1 + d_1) t^{P1} + (\mu_2 + d_2) t^{P2}$$
 - These differences can be incorporated into meta-analyses or network meta-analyses (NMAs); for treatment i , pooled estimates for $d_{0,i}$, $d_{1,i}$, and/or $d_{2,i}$ can be produced relative to a reference treatment¹
- These models produce time-dependent hazard ratios (HRs) and therefore are used in networks for which the proportional hazards assumption does not hold
- Despite the benefits of using FP models, there are some challenges in the modeling process
 - Fitting data to all possible model forms produces a large number of candidate models
 - Functional forms that fit data well in the early course of follow-up may have clinically implausible behavior in the tails (when evidence is based on a small at-risk population with great uncertainty) and during extrapolated periods
 - In networks of evidence with heterogeneous durations of follow-up, care must be taken in distinguishing between time periods for which HRs were observed and extrapolated; the clinical plausibility of the model forms should be evaluated
 - The deviance information criterion (DIC), despite its widespread use, suffers from a lack of consistency and an arguably poor theoretical justification²
 - Therefore, it is unclear whether it sufficiently penalizes FP model complexity; it can thus lead to overfitting, particularly in the tails. Furthermore, it cannot be applied to extrapolated periods

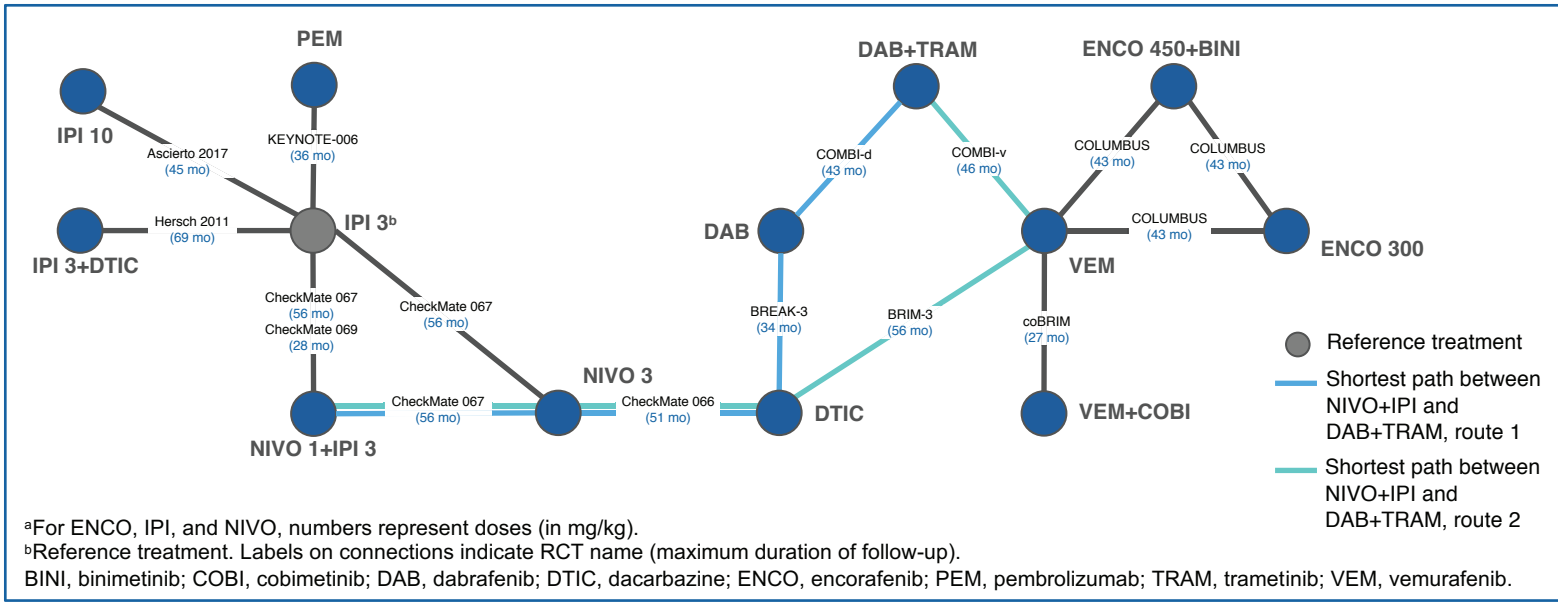
Objective

- To present a model-selection heuristic that incorporates clinical plausibility of model extrapolations and involves transparent reporting of observed and extrapolated periods
 - An FP-based NMA in first-line treatment of advanced melanoma served as an example

Methods

- Evidence base**
- The evidence base was identified through a systematic review of randomized controlled trials (RCTs) assessing the efficacy and safety of treatments for treatment-naïve patients with advanced unresectable stage III or IV melanoma³
 - The network formed by the RCTs is presented in **Figure 1**
 - A time-varying HR analysis was conducted, as the proportional hazard assumption did not appear to hold
 - We distinguished between observed and extrapolated periods for each pair of comparators in the network
 - First, for each edge in the network, the maximum directly observed period was established as the maximum duration of follow-up across all RCTs in that particular connection (denoted below each RCT name)
 - Second, the shortest path (the path connecting the nodes with the fewest possible edges) between each pair of comparators was established
 - Third, as a common duration of follow-up, the minimum of the directly observed periods along the shortest network path was calculated; subsequent time points were considered as extrapolations
 - In cases in which ≥ 2 paths were shortest (eg, route 1 and route 2 in **Figure 1**), the route with the longest common duration of follow-up was taken
 - As an example, the extrapolated period for nivolumab plus ipilimumab (NIVO+IPI) versus dabrafenib plus trametinib (DAB+TRAM) begins after 46 months, which is the common duration of follow-up time along route 2 in **Figure 1**

Figure 1. Network of evidence for treatment-naïve advanced unresectable melanoma^a



Fractional polynomial models

- Using digitally reconstructed individual patient-level data for overall survival, we fit Weibull-based FP models (where shape 1, power $P1 = 0$) and Gompertz-based FP NMA models (where shape 1, power $P1 = 1$)⁴
- Treatment effects were placed on the scale parameter (d_0), representing proportional hazards (complexity level 1; **Figure 2**)
- To each model, we added further complexity (**Figure 2**)
 - Level 2: treatment effects were added to the shape 1 (ie, time-related) parameter (d_1)
 - Level 3: a second shape parameter was added (shape 2; $P2$ powers chosen from $\{-1, -0.5, 0, 0.5, 1\}$)
 - Levels 4a and 4b: both shape parameters were retained and treatment effects were added to either shape 1 (d_1) or shape 2 (d_2)
 - Level 5: treatment effects were added to both shape parameters, d_1 and d_2
- Model families were defined by the choice of $P1$ or $P2$
- As there was typically only 1 RCT connecting any 2 given nodes in the network (**Figure 1**), fixed-effect models were selected a priori

Figure 2. Fractional polynomial model development and candidate models

Complexity	Scale	Shape 1 (P1)	Shape 2 (P2)	Number of combinations ^a
1	$(\mu_0 + d_0)$	$\mu_1 \ln(t)$	None	1
	$(\mu_0 + d_0)$	$\mu_1 t$	None	1
2	$(\mu_0 + d_0)$	$(\mu_1 + d_1) \ln(t)$	None	1
	$(\mu_0 + d_0)$	$(\mu_1 + d_1) t$	None	1
3	$(\mu_0 + d_0)$	$\mu_1 \ln(t)$	$\mu_2 t^{P2a}$	5
	$(\mu_0 + d_0)$	$\mu_1 t$	$\mu_2 t^{P2a}$	5
4a	$(\mu_0 + d_0)$	$(\mu_1 + d_1) \ln(t)$	$\mu_2 t^{P2a}$	5
	$(\mu_0 + d_0)$	$(\mu_1 + d_1) t$	$\mu_2 t^{P2a}$	5
4b	$(\mu_0 + d_0)$	$\mu_1 \ln(t)$	$(\mu_2 + d_2) t^{P2a}$	5
	$(\mu_0 + d_0)$	$\mu_1 t$	$(\mu_2 + d_2) t^{P2a}$	5
5	$(\mu_0 + d_0)$	$(\mu_1 + d_1) \ln(t)$	$(\mu_2 + d_2) t^{P2a}$	5
	$(\mu_0 + d_0)$	$(\mu_1 + d_1) t$	$(\mu_2 + d_2) t^{P2a}$	5

^aThe number of combinations is based on setting $P2$ to each value within the set $\{-1, -0.5, 0, 0.5, 1\}$.

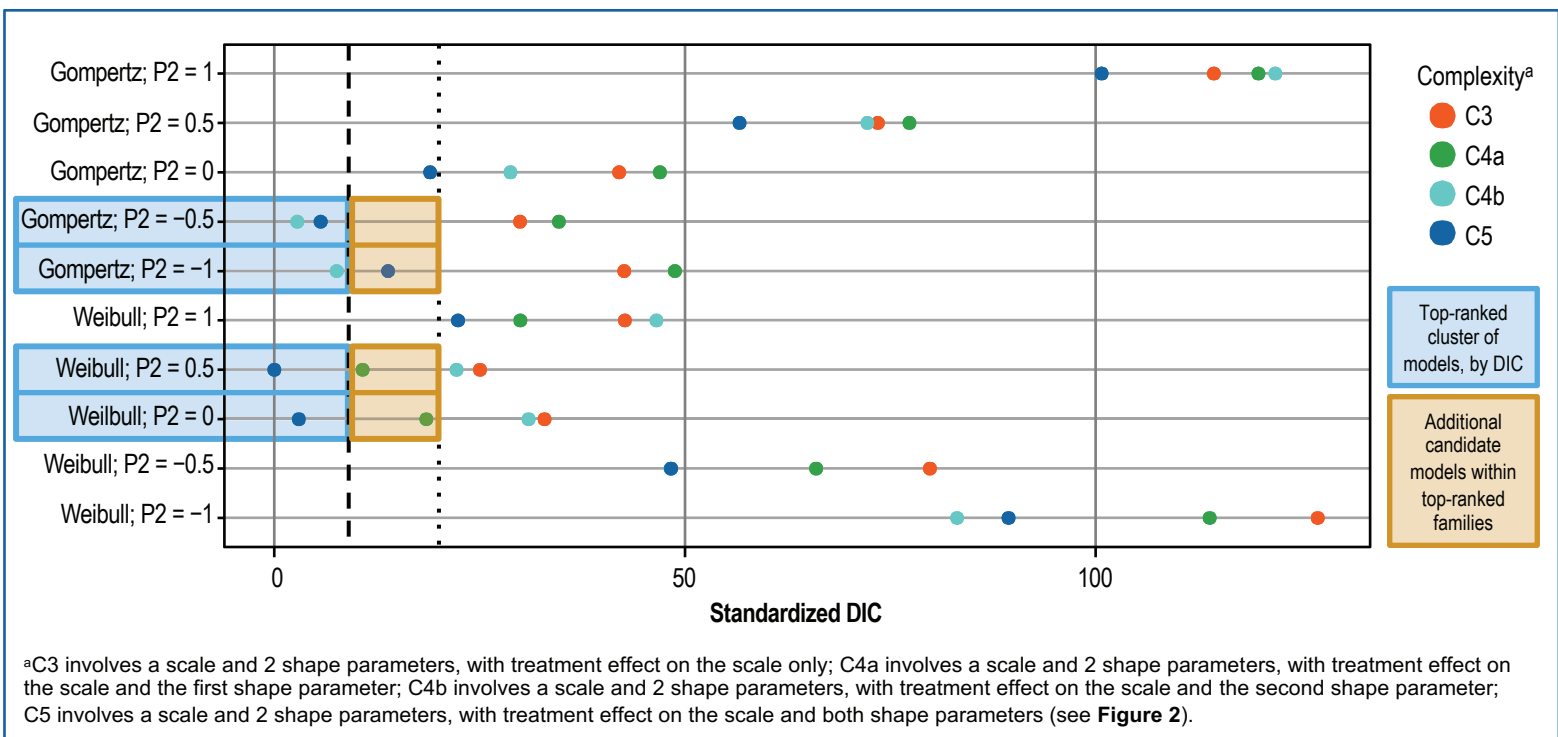
Model-selection heuristic

- The model-selection heuristic involved ranking models according to 4 criteria
 - DIC:** The DIC for each model was standardized by subtracting the smallest DIC among all models. (Models in the top-ranked cluster [in this example, the top 5 models] according to DIC were retained as candidate models)
 - Additional model complexity penalties:** As the DIC may insufficiently penalize for complexity, we also retained less complex models from the same families identified by DIC alone. (To limit the number of candidate models, we excluded models with a standardized DIC > 20)
 - Visual inspection of observed versus modeled output:** Study-specific FP model survival curves were overlaid upon observed Kaplan–Meier (KM) curves to visualize deviations between observed and parameterized curves. (For transparency, extrapolations beyond the indirectly observed period were distinguished from observed periods using dashed lines)
 - Clinical plausibility of extrapolation periods:** For all time periods beyond the observed period, the clinical plausibility was evaluated based on observed data from other drugs within the same class and indication

Results

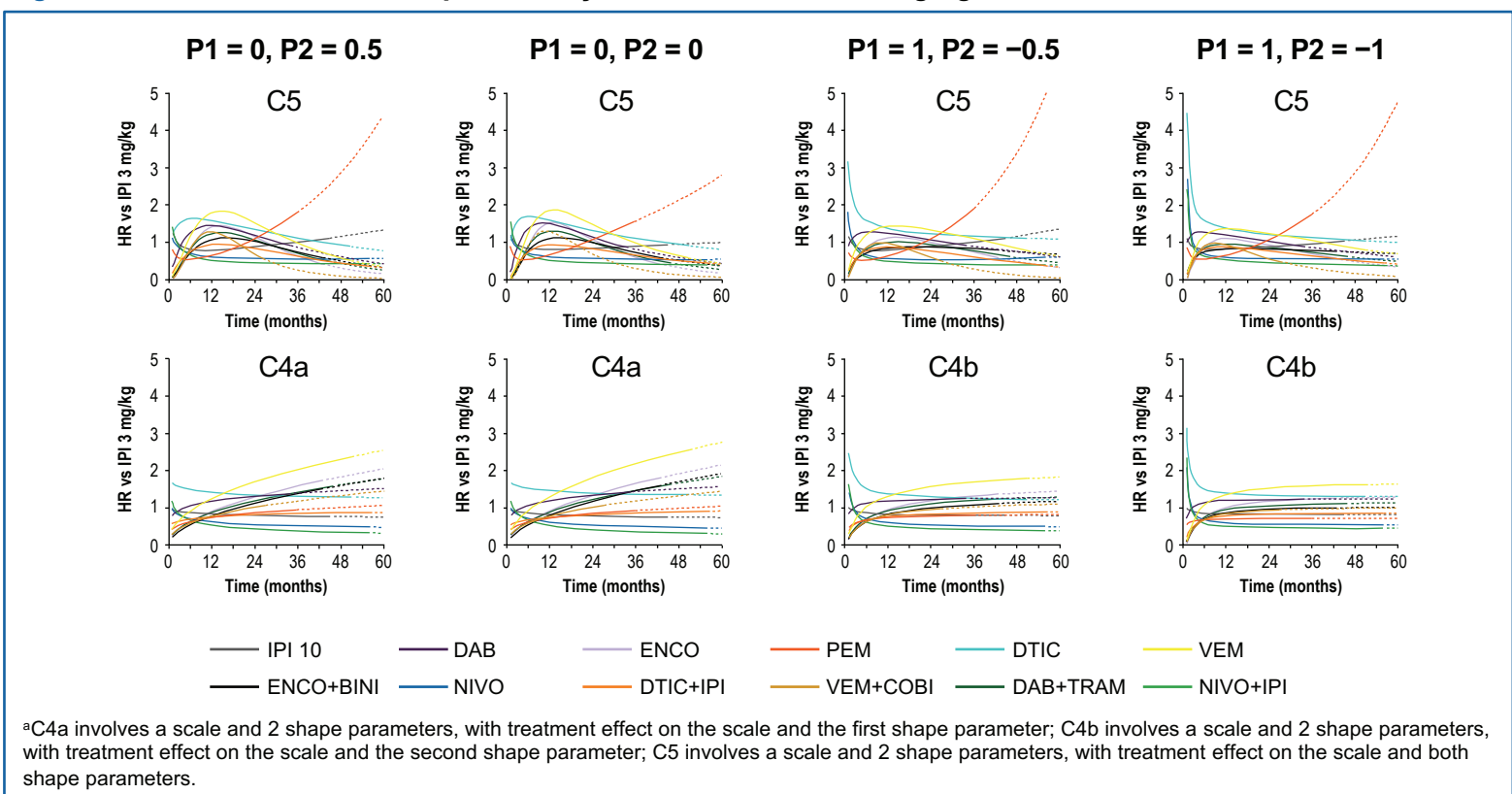
- In total, 44 fixed-effect models were run
- According to the DIC, the 5 top-ranked models included 2 Weibull-based FP model families (shape 2, powers $P2 = 0.5$ and $P2 = 0$) and 2 Gompertz-based FP models (shape 2, powers $P2 = -1$ and $P2 = -0.5$) (**Figure 3**; blue shading)
 - Models with complexity levels 1 and 2 had standardized DICs > 350 (results not shown)
- Additional models from the same family as these 5 top-ranked models, whose standardized DICs were < 20, were also retained as candidate models (**Figure 3**; gold shading)

Figure 3. DIC by model family



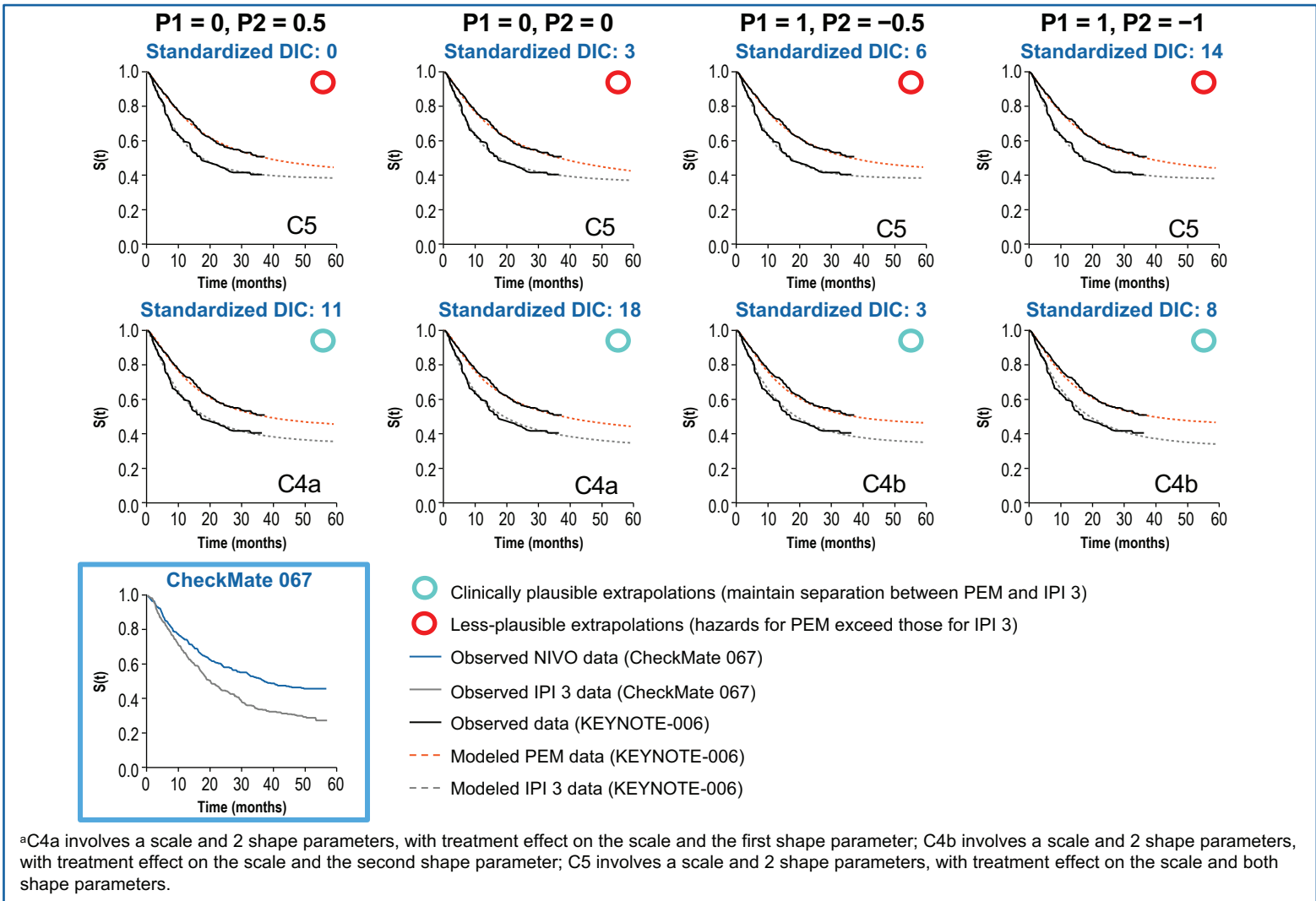
- For each candidate model, plots of the estimated HRs relative to the reference treatment (IPI 3) were used to distinguish between the observed and extrapolated periods (**Figure 4**)
- Visual inspection of these HRs revealed that the most complex models (C5) showed clinically implausible within-drug class heterogeneity in the extrapolated periods when compared with simpler models (C4a or C4b)
- Specifically regarding trends in extrapolated HRs versus IPI 3
 - For PEM, **extrapolated** HRs differed markedly from the **observed** HRs for NIVO
 - For VEM+COBI, **extrapolated** HRs differed from the **observed** HRs for other BRAF+MEK inhibitor combinations

Figure 4. Evaluation of clinical plausibility of HRs versus IPI 3 mg/kg for candidate models^a



- When reviewing the study-specific FP models, compared with observed data, differences were noted in how each FP model fit the tails and extrapolation periods (eg, the extrapolation period for KEYNOTE-006 is displayed in **Figure 5**)
 - In the complexity-level C5 models, the KM tails and extrapolation periods for PEM versus IPI 3 were converging (corresponding to an HR > 1 for PEM vs IPI 3), whereas the level C4a and C4b models maintained separation (corresponding to an HR of ~ 1)
 - The C5 models were more heavily influenced by events near the end of KEYNOTE-006 RCT follow-up, when the population at risk was small and mostly censored. (By 36 months, the numbers at risk were 12 patients and 4 patients for the PEM and IPI 3 arms, respectively)
 - These trends evident in the C5 models were inconsistent with observed trends in the same period for NIVO versus IPI 3
- The heuristic guided the final model choice toward less complex models with similar DICs, but without the C5 level of complexity

Figure 5. Visual inspection of extrapolation periods for KEYNOTE-006^a



Discussion

- Our heuristic is an integrated model-selection framework combining both internal validity using the statistical measures of a model fit to the observed data and external validity of the tail and extrapolation periods
 - This is consistent with good-practice guidance for survival extrapolations in cost-effectiveness models⁵
- Our findings highlight the caveat that the most complex (C5) models may overfit to the data at the end of the follow-up period when the number of patients at risk is typically low; such overfitting may yield clinically implausible extrapolations
 - Selecting models of slightly lower complexity, with 2 shape parameters but treatment effects on only 1 of these parameters (eg, C4a, C4b), appeared to be a more prudent approach
- Our heuristic was based on an NMA involving only 36 months of follow-up data from KEYNOTE-006. Recently, 5-year results of KEYNOTE-006 were released, and the newly observed data were consistent with the clinically plausible C4a and C4b extrapolations; the final FP model in the updated NMA was C4b ($P1 = 1$; $P2 = -1$)^{3,6}
- Clear demarcation of observed and extrapolated periods provided greater transparency in reporting, ensuring that the latter are not misrepresented, particularly in networks with heterogeneous follow-up times
 - The clarification that the extrapolated period begins at the shortest observed period **along the network path** is important, as this may be shorter than the observed period for 2 individual comparators
- Our heuristic was not prescriptive. Further research across multiple endpoints and indications is needed to ensure a specific predefined approach to model selection can be followed to minimize subjectivity in the model-selection process

Conclusions

- FP models with 2 shape parameters and treatment effects on both (C5) may overfit the tails of the follow-up period, when numbers at risk tend to be small; less complex models (eg, C4a, C4b) can provide comparable model fit with greater clinical plausibility in the tails and extrapolation periods
- A combination of DIC, visual inspections, and consideration of external validity should be used as part of the model-selection heuristic
- When reporting time-specific HRs, a clear demarcation of observed and extrapolated periods should be used

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